Towards an Automatic Translation of Colored Petri Nets to Maude Language

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Abstract—Colored Petri Nets (CPN) are very known kind of high level Petri nets. With sound and complete semantics, rewriting logic is one of very powerful logics in description and verification of non-deterministic concurrent systems. Recently, CPN semantics are defined in terms of rewriting logic, allowing us to build models by formal reasoning. In this paper, we propose an automatic translation of CPN to the rewriting logic language Maude. This tool allows graphical editing and simulating CPN. The tool allows the user drawing a CPN graphically and automatic translating the graphical representation of the drawn CPN to Maude specification. Then, Maude language is used to perform the simulation of the resulted Maude specification. It is the first rewriting logic based environment for this category of Petri Nets.

Keywords—Colored Petri Nets, Rewriting Logic, Maude, Graphical Edition, Automatic Translation, Simulation.

I. INTRODUCTION

Colored Petri Nets (CPN) are very known kind of high level Petri nets. Rewriting logic has sound and complete semantics [6] and it is considered as one of very powerful logics in description and verification of non-deterministic concurrent systems. Also, the rewriting logic language Maude [7] is considered as one of very powerful languages in specification, programming and verification of non-deterministic concurrent systems. CPN semantics are defined in terms of rewriting logic [8], allowing us to build models by formal reasoning. Rewriting logic gives to CPN a simple, more intuitive and practical textual version to analyze, without loosing formal semantic (mathematical rigor, formal reasoning).

However, Maude system offers textual way to the user to create and deal with CPN system. Execution under Maude system is done by using command prompt style. In this case, we lose the graphical aspect of CPN formalism which is important for the clarity, simplicity and readability of a system description.

In this paper, we propose a simple tool for automatic translation of CPN to Maude language. This tool includes also graphical edition and simulation of CPN by using Maude. The proposed tool is a simple tool to well exploit the advantages of CPN formalism such as graphical aspect, simplicity and readability that are important for preliminary description in system development. This tool acts as follows: it allows to the user to edit graphically a CPN and then converts the graphical representation to its equivalent description in Maude. Thereafter, the tool calls the Maude system for the execution of the CPN and reconverts the resulting marking described in Maude to a graphical representation. This step allows us to perfectly exploit all advantages of Maude described above. We notice that the integration of CPN in rewriting logic facilitated the development of such environment. With the help of a CPN example, we will compare the simulations of the example under Maude system and our tool. One of the objectives of this work is to fully exploit the power of this logic and Maude language. Maude is simple, very expressive and efficient [4].

Of course, in the context of Petri nets simulation and analysis, many tools have been developed. Most of these tools for CPN are implemented using the known imperative languages like Java, C++. We mention here some much known tools that are proposed for CPNs. CPN/Tools [2] is a major redesign of the Design/CPN [9] tool for editing, simulation and state space analysis of Colored Petri Nets. CPN Tools [10] is a tool for editing, simulating and analyzing Colored Petri Nets. The functionality of the simulation engine and state space facilities are similar to the corresponding components in Design/CPN.

Let’s note that these proposed environments are mature and include many analysis tools. We can not compare our tool with these environments in terms of services provided. But, our tool is special because it is the first one which offers an automatic translation of CPN to Maude. This integration allows to the CPNs to get a sound and complete semantic especially the true concurrency description. Our work concerning graphic and edition and simulation of Petri nets based Maude is not limited to just CPNs. We already proposed the development of graphic simulator for ordinary Petri nets and for another category of algebraic Petri nets ECATNets by using Maude [3]. This work constitutes a way of important investigation. We want to use, in fact, only one platform (Maude) to allow the communication between systems developed beforehand by using different kinds of Petri nets. This can be carried out by an automatic generation of Maude descriptions starting from ordinary Petri nets, ECATNets, CPN and other Petri nets models which are integrated in Maude.

The remainder of this paper is organized as follows: in section 2, we present a short outline on the rewriting logic and

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Maude. We give a brief introduction on CPN formalism and their integration in rewriting logic in section 3 through a simple example. Most important functionalities of our simple application are illustrated in section 4. We show also in this section how we run our application with the help of the example. Software and hardware used in developing our application are mentioned in section 5. Finally, section 6 concludes the paper.

II. REWRITING LOGIC REVIEW

In rewriting logic, each concurrent system is represented by a rewrite theory \( \mathcal{R} = (\Sigma, E, L, R) \). Its static structure is described by the signature \( (\Sigma, E) \), whereas its dynamic structure is described by the set of labelled rewrite rules \( R \), which are applied modulo the equation \( E \). An important consequence of the rewriting logic definition is that a rewrite theory \( \mathcal{R} = (\Sigma, E, L, R) \) can be viewed as an executable specification of the concurrent system that it formalizes. In this section we recall the basic definitions of the rewriting logic.

A labelled rewrite theory \( \mathcal{R} \) is a 4-tuple \( \mathcal{R} = (\Sigma, E, L, R) \) where \((\Sigma, E)\) is a signature; \( \Sigma \) is the sorts set and operators and \( E \) is a set of \( \Sigma \)-equations. The signature \((\Sigma, E)\) is an equational theory which describes the particular algebraic structure of the states of a system (multiset, binary tree, etc.) which are distributed according to this same structure. \( R \subset L \times (\tau \Sigma, E) \) is the set of pairs whose first component is a label and the second is a pair of \( E \)-equivalence classes of terms, with \( X = \{x_1, \ldots, x_n, \ldots\} \) a countable infinite set of variables. The elements of \( R \) are called conditional rewrite rules. They describe the elementary and local transitions in a concurrent system. Each rewrite rule corresponds to an action being able to occur, simultaneously, with other actions. The rewriting will operate on equivalence classes of terms, modulo a set of equations \( E \). For a rewrite rule \( (r, ([t_1],[t']_1), ([u_1],[v_1]), \ldots, ([u_k],[v_k])) \) we use the notation, \( r : [t] \rightarrow [t'] \) if \( \forall u \in \{u_1, \ldots, u_k\} \) and \( \forall v \in \{v_1, \ldots, v_k\} \), where \([t]\) represents the equivalence class of the term \( t \). A rule \( r \) expresses that the equivalence class containing the term \( t \) is changed to the equivalence class containing the term \( t' \) if the conditional part of the rule, \([u_1] \rightarrow [v_1] \land \ldots \land [u_k] \rightarrow [v_k] \), is verified.

Given a labeled rewrite theory \( \mathcal{R} \), we say that \( \mathcal{R} \) entails a sequent \( r : [t] \rightarrow [t'] \), or that \( r : [t] \rightarrow [t'] \) is a (concurrent) \( \mathcal{R} \)-rewrite and write \( \mathcal{R} \vdash r : [t] \rightarrow [t'] \) iff \( [t] \rightarrow [t'] \) is derivable from the rules in \( \mathcal{R} \) by a finite application of the deduction rules (reflexivity, transitivity, congruence, and replacement) of rewriting logic.

A rewrite theory is a static description of a concurrent system. Its semantics is defined by a mathematical model which describes its behavior. The model for a given labelled rewriting theory \( \mathcal{R} = (\Sigma, E, L, R) \) is a category \( \tau \Sigma, E(X) \) whose objects (states) are equivalence classes of terms \([t] \in \tau \Sigma, E(X)\) and whose morphisms (transitions) are equivalence classes of proof-terms representing proofs in rewriting deduction.

- **Reflexivity.** For every \( [t] \in \tau \Sigma, E(X) \): \( [t] \rightarrow [t] \)
- **Congruence.** For every \( f \in \Sigma, n \in \mathbb{N} : \)
  \[
  [t_1] \rightarrow [t'_1] \quad \ldots \quad [t_k] \rightarrow [t'_k] \\
  \left[ f(t_1, \ldots, t_k) \right] \rightarrow \left[ f(t'_1, \ldots, t'_k) \right]
  \]
- **Replacement.** For every rewriting rule \( r : ([t_1], \ldots, [t_n]) \rightarrow ([t'_1], \ldots, [t'_n]) \) in \( \mathcal{R} \),
  \[
  [w_1] \rightarrow [w'_1] \quad \ldots \quad [w_n] \rightarrow [w'_n]
  \]
  such that \( r([w'/x]) \rightarrow [t'/w'] \)
  \( t'(w/x) \) indicates the simultaneous substitution of \( w_i \) for \( x_i \) in \( t \).
- **Transitivity.** \( [t_1] \rightarrow [t_2] \quad [t_2] \rightarrow [t_3] \)
  \( [t_1] \rightarrow [t_3] \)

A. Maude Language

Maude is a specification and programming language based on rewriting logic. Maude is simple, expressive and efficient. It is rather simple to program with Maude, considering that it belongs to the declarative programming languages. It is possible to describe using Maude different types of applications, from prototyping ones to high concurrent applications. Maude is a competitive language in terms of execution and simulation with imperative programming languages [4]. Three types of modules are defined in Maude. The functional modules, the system modules and the object-oriented modules which can, in fact, be reduced to system modules. Because we do not need object-oriented modules here, so we do explain only system and functional modules.

Functional Modules. The functional modules define data types and related operations, which are based on equations theory. By using equations like simplification rules, each expression called term could be evaluated to its reduced form called canonical representation. All the equal terms by means of equations form an equivalence class. The canonical form represents all the terms of the same equivalence class. The set of all the equivalence classes of the ground (i.e., variable-free) terms constitutes a denotational model for a functional module (initial algebra). Equations in a functional module are oriented. They are used from left to right and the final result of the simplification of an initial term is unique independently of the order in which these equations are applied. In addition to equations, this type of modules supports membership’s axioms. These axioms impose constraints so that a term is of a particular type if a certain condition is satisfied. This condition is a conjunction of equations and unconditional tests of memberships.

System Modules. The system modules define the dynamic behavior of a system. This type of module augments the functional modules by the introduction of rewriting rules. This type of module offers a maximum degree of concurrency. A system module describes a “rewriting theory” which includes kinds, operations and three types of statements: equations, memberships and rewriting rules. These three types of statements can be conditional. A rewriting rule specifies a “local concurrent transition” which can proceed in a system.
The execution of such transition, specified by the rule, can take place when the left part of a rule matches to a portion of the global state of the system and the condition of the rule is valid.

III. COLORED PETRI NETS

Colored Petri nets (CPN) are very known and we can find easily their definition in the literature. Among these definitions we have the following one : a CPN is a tuple \( \text{CN} = [P, T, F, \psi, A, m_0] \) such that:

1. \([P, T, F]\) is a net, i.e. \(P\) and \(T\) are finite and disjoint sets called places and transitions, respectively, and \(F\) is a relation \(F \subseteq (P \times T) \cup (T \times P)\), the elements of which are called arcs;
2. \(\psi\) assigns a countable set of colors to every element of \(P \cup T\);
3. \(A\) assigns to every \([x, y] \in F\) a mapping which in turn assigns a finite semi-positive multiset over \(\psi(p)\) to every color in \(\psi(t)\) where \(p\) is the place of \(x\) and \(y\) and \(t\) is the transition of \(x\) and \(y\);

\(m_0\) is a marking which assigns a finite semi-positive multi-set over \(\psi(p)\) to every \(p \in P\). \(m_0\) is called the initial marking.

A. Representation of CPN in Maude

In this section, we will explain through a very simple example how to express a CPN in Maude language according to [8]. For domains of colors \(C_1 = \{A, B\}\) and \(C_2 = \{C, D\}\), we have the simple CPN in the figure 1.

Let’s take an initial marking such that \(M_0(p_1) = 2A + 2B\) and \(M(p_2)\) is empty. In the sequel, we describe how to obtain the equivalent Maude code of this CPN example. First we create a sort MS to describe a general multi-set, the constant empty for an empty multi-set and the operation without name (\(\_\_\\) ) (the underlines indicate the two parameters of this operation). This operation is commutative, associative and has as an element identity empty. This operation allows the construction of any multi-set including empty multi-set (empty).

\[\text{mod} \ \text{BASIC}\]
\[\text{sort} \ \text{MS}\ .\]
\[\text{op} \ \text{empty} : \rightarrow \text{MS} .\]
\[\text{op} \ \_\_ : \text{MS} \ \rightarrow \text{MS} \ [\text{assoc comm. id: empty}] .\]
\[\text{endm}\]

\(m_0\) is a marking which assigns a finite semi-positive multi-set over \(\psi(p)\) to every \(p \in P\). \(m_0\) is called the initial marking.

\[\text{mod} \ \text{CPN}\]
\[\text{pr} \ \text{BASIC}\ .\]
\[\text{sorts} \ C_1 \ C_2 .\]
\[\text{subsort} \ C_1 < \text{MS} . \ \text{subsort} \ C_2 < \text{MS} .\]
\[\text{ops} \ A \ B : \rightarrow \ C_1 . \ \text{ops} \ C \ D : \rightarrow \ C_2 .\]
\[\text{op} \ P_1 : C_1 \rightarrow C_1 . \ \text{op} \ P_2 : C_2 \rightarrow C_2 .\]
\[\text{rl} \ [T_1] : P_1(A) P_1(B) => P_2(C) P_2(D) .\]
\[\text{endm}\]
\[\text{rew} \ P_1(A) P_1(A) P_1(B) P_1(B) .\]

B. Execution of CPN Example under Maude System

We find an example of initial state and the result of its unlimited rewriting in figure 2.
**A. Graphical User Interface**

In this step, user can create his own CPN system. In the figure 4, we find principal window, on what the previous example of CPN is created. In this interface, we show that our application contains from left to right the following options: ToolBar, New, Open, Save, Print, Code Generation and Exit. So, New to create new file containing new CPN, Open to open existent file, Save to save current file, Print for printing current file and Exit to close the tool. In addition to these options, we find two other options ToolBar and Code Generation. ToolBar includes necessary options to create CPN, in the tool bar ‘Draw’, we have:

- Circle to create new place, rectangle to create new transition, arcs to create new arcs linking places and transitions;
- D for Delete : to delete a place, a transition or an arc;
- S for Sub-domain : to create or modify a sub-domain for a selected place;
- M for Marking : to create or modify a marking in a selected place;
- C for Arc Condition : to create or modify condition arc.

After creating graphically a CPN, user can click on the icon of Code Generation to generate the corresponding Maude code.

In this figure, we find in the right of the place P1 the set A, B which is the color domain of this place and the multi-set 2A+2B which represents the current marking of P1 (initial marking in this case).

**B. Automatic Translating CPN Graphical Representation to Maude Description**

This step has the graphical representation of CPN model as input. It consists of translating this representation into an equivalent Maude description. In fact, this representation contains on one hand the structure of the CPN and on the other hand, the initial state of this CPN. The output of this step is two elements: an equivalent code in Maude of CPN structure and an initial state in Maude syntax. After clicking on ‘code generation’ option, another new menu occurs (figure 5). By clicking on the option code generation, we get the generated code equivalent in Maude to CPN according to the translation proposed in [8]. We have to click on ‘watch code’ option to get the Maude code displayed on the right of the screen as depicted in the figure 5.

**C. Simulation**

The output of the previous step is the input of this one. To do simulation, the simulator needs from the user the initial state of the CPN. Simulation consists of transforming this initial state to another by doing one or many rewriting actions.
Therefore, in addition to initial state, the user may give to the simulator the number of rewriting steps if (he/she) wants to check intermediary states. If this number is not given, the simulator continues the rewriting operation until reaching final state. In figure 5, we asked the application to perform the simulation on the previous initial marking without indicating the number of rewriting steps. The Result (final state) of the simulation is given in the same manner as initial one. We notice that infinite case is possible. Let’s go back to the example, after displaying the Maude code equivalent to CPN, we can now execute the code by clicking ‘code execution’ option. In our case, the unlimited rewriting of the example gives the result in the figure 6. Let’s note that we exposed the result marking in graphical manner (on the CPN) and in textual way in Maude language.

**VI. Conclusion**

In this paper, we proposed a simple rewriting logic based tool for CPN edition and simulation. This application includes tasks like: edition, automatic translation of CPN to Maude and simulation. The editor allows the user to draw a CPN graphically; the automatic translator allows translating the graphical representation of the drawn CPN to a Maude specification. Then the rewriting logic language Maude is used to perform the simulation of the resulted Maude specification. We think that the power of Maude in terms of specification, programming, simulation and verification in plus of the CPN integration in Maude, implies that there is no need to translate CPN to several languages for such requirements. Therefore, we avoid any mistranslation of CPN in several languages and thus any risks about their semantic loss.

The CPN’s tool will be extended by adding other tools. The tools planned to be integrated in this application will be developed under Maude system. This tool may be enriched by all already proposed tools for Maude including coherence checker for system modules [5] or and inductive theorem prover [1] to check functional properties modules’ properties. The objective of the integration of such tools is making easy the utilization of these tools.

Our work concerning graphic and edition and simulation of Petri nets based Maude is not limited to just CPNs. We already proposed the development of graphic simulator for ordinary Petri nets and for another category of algebraic Petri nets ECATNets by using Maude [3]. This work constitutes a way of important investigation. We want to use, in fact, only one platform (Maude) to allow the communication between systems developed beforehand by using different kinds of Petri nets. This can be carried out by an automatic generation of Maude descriptions starting from ordinary Petri nets, ECATNets, CPN and other Petri nets models which are integrated in Maude.

Let’s note that in the same paper [8], authors propose also an integration of algebraic Petri nets (APN) in rewriting logic. In this way, we plan also performing a graphic interface of this kind of Petri Nets with an automatic translation of APN to Maude language for simulation.
REFERENCES


